Mining socio-political and socio-economic signals from social media content

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Structure of the presentation

- 1. Introductory remarks
- 2. Collective inference tasks
 Mining emotions
 Modelling voting intention
- 3. Personalised inference tasks
 - Occupational class
 - Income
 - Socioeconomic status
- 4. Concluding remarks

Context and motivation



How can we use online user-generated content to enhance our understanding about our world?

Context and motivation



How can we use online user-generated content to enhance our understanding about our world?

About Twitter



And what about the statistical significance of the computed statistical significance? *#inception_in_statistics*← Reply Delete ★ Favorite
RT if you love Justin Bieber. Delete ur account if you don't.
← Reply Retweet ★ Favorite

 50
 1

 RETWEETS
 FAVORITE

Why do I feel so happy today hihi. Bedtimeeee, good night. Yey thank You Lord for everything. Answered prayer ♥

🛧 Reply 🔁 Retweet 🔺 Favorite

i think i have the flu but i still look fabulous



About Twitter



And what about the statistical significance of

- the **140 characters** per published status (*tweet*)
- Re > users can follow and be followed
 - > embedded usage of topics (using #hashtags)
 - > user interaction (re-tweets, @mentions, likes)
 - > real-time nature
- Wh biased demographics (13-15% of UK's population, age bias etc.)
- ♠ Re > information is noisy and not always accurate

i think i have the flu but i still look fabulous



Inferring collective information from user-generated content

•····• mood / emotions •····• voting intention

Lampos (Ph.D. Thesis, 2012) Lansdall-Welfare, Lampos & Cristianini (WWW 2012) Lampos, Preotiuc-Pietro & Cohn (ACL 2013)

Emotion taxonomies and quantification

- > WordNet Affect
- > Linguistic Inquiry and Word Count (LIWC)

(Strapparava & Valitutti, 2004; Pennebaker et al., 2001, 2007)

'Emotional' keywords, representing
+ anger, e.g. angry, irritate
+ fear, e.g. fearful, afraid
+ joy, e.g. cheerful, enthusiastic
+ sadness, e.g. depressed, gloomy
+ plus other emotions

Simply — *but maybe not good enough!* — we compute the **mean keyword frequency score** per emotion

Emotion taxonomies and quantification

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Circadian emotion patterns from Twitter (UK)



24h emotion patterns for 'joy' and 'sadness' for summer and winter with 95% confidence intervals

'Joy' time series based on Twitter (UK)



Clear peaking pattern during XMAS or other annual celebrations (Valentine's Day, Easter)

Recession, riots, and Twitter emotions (UK)



Difference in mean mood score 50 days prior and after each date; **peaks** indicate **increase in mood change**

Inferring voting intention — Data sets

United Kingdom

- + **3** political **parties** (Conservatives, Labour, Lib Dem)
- + **42,000** Twitter **users** distributed proportionally to UK's regional population figures
- + 60 million tweets, 80,976 1-grams
- + 240 polls from 30 Apr. 2010 to 13 Feb. 2012

Austria

- + 4 political parties (SPO, OVP, FPO, GRU)
- + 1,100 active Twitter users selected by political scientists
- + 800,000 tweets, 22,917 1-grams
- + 98 polls from 25 Jan. to 25 Dec. 2012

Regularised text regression

observations responses weights, bias

$$\mathbf{x}_{i} \in \mathbb{R}^{m}, i \in \{1, \dots, n\} \quad - \quad \mathbf{X}$$
$$y_{i} \in \mathbb{R}, i \in \{1, \dots, n\} \quad - \quad \mathbf{y}$$
$$w_{j}, \beta \in \mathbb{R}, j \in \{1, \dots, m\} \quad - \quad \mathbf{w}_{*} = [\mathbf{w}; \beta]$$

$$f(\mathbf{x}_i) = \mathbf{x}_i^{\mathrm{T}} \mathbf{w} + \beta$$

Elastic Net (*Zou & Hastie, 2005*)



L1-norm L2-norm

Regularised text regression

observations responses weights, bias

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$$f(\mathbf{x}_i) = \mathbf{x}_i^{\mathrm{T}} \mathbf{w} + \beta$$

Elastic Net (Zou & Hastie, 2005)

$$\operatorname{argmin}_{\mathbf{w},\beta} \left\{ \sum_{i=1}^{n} \left(y_i - \beta - \sum_{j=1}^{m} x_{ij} w_j \right)^2 + \lambda_1 \sum_{j=1}^{m} |w_j| + \lambda_2 \sum_{j=1}^{m} w_j^2 \right\}$$

L1-norm L2-norm

Bilinear (users+text) regularised regression







$$\operatorname{argmin}_{\mathbf{u},\mathbf{w},\beta} \left\{ \sum_{i=1}^{n} \left(\mathbf{u}^{\mathrm{T}} \mathbf{Q}_{i} \mathbf{w} + \beta - y_{i} \right)^{2} + \psi(\mathbf{u},\theta_{\mathbf{u}}) + \psi(\mathbf{w},\theta_{\mathbf{w}}) \right\}$$

where

$$\psi(\mathbf{x}, \lambda_1, \lambda_2) = \lambda_1 \|\mathbf{x}\|_{\ell_1} + \lambda_2 \|\mathbf{x}\|_{\ell_2}^2$$

Training bilinear elastic net (BEN)

$$\operatorname{argmin}_{\mathbf{u},\mathbf{w},\beta} \left\{ \sum_{i=1}^{n} \left(\mathbf{u}^{\mathrm{T}} \mathbf{Q}_{i} \mathbf{w} + \beta - y_{i} \right)^{2} + \psi(\mathbf{u},\theta_{\mathbf{u}}) + \psi(\mathbf{w},\theta_{\mathbf{w}}) \right\}$$

Biconvex problem

- + fix **u**, learn **w** and vice versa
- + iterate through convex optimisation tasks

Large-scale solvers in SPAMS (*Mairal et al., 2010*)

Global objective function during training (*red*)

Corresponding prediction error on held out data (*blue*)



Training bilinear elastic net (BEN)

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Bilinear and multi-task regression

tasks	$ au \in \mathbb{Z}^+$		
users	$p \in \mathbb{Z}^+$		
observations	$\mathbf{Q}_i \in \mathbb{R}^{p imes m},$	$i \in \{1, \ldots, n\}$ —	\mathcal{X}
responses	$\mathbf{y}_i \in \mathbb{R}^{ au},$	$i \in \{1, \ldots, n\}$ —	Y
weights, bias	$\mathbf{u}_k, \mathbf{w}_j, \boldsymbol{\beta} \in \mathbb{R}^{ au},$	$k \in \{1, \dots, p\} -$	$\mathbf{U},\mathbf{W},oldsymbol{eta}$
		$j \in \{1, \ldots, m\}$	

$$f\left(\mathbf{Q}_{i}\right) = \operatorname{tr}\left(\mathbf{U}^{\mathrm{T}}\mathbf{Q}_{i}\mathbf{W}\right) + \beta$$



Bilinear Group L_{2,1} (BGL)



$$\operatorname{argmin}_{\mathbf{U},\mathbf{W},\boldsymbol{\beta}} \left\{ \sum_{t=1}^{\tau} \sum_{i=1}^{n} \left(\mathbf{u}^{\mathrm{T}} \mathbf{Q}_{i} \mathbf{w}_{t} + \beta_{t} - y_{ti} \right)^{2} + \lambda_{u} \sum_{k=1}^{p} \|\mathbf{U}_{k}\|_{2} + \lambda_{w} \sum_{j=1}^{m} \|\mathbf{W}_{j}\|_{2} \right\}$$

- + a nonzero weighted feature (user or word) is encouraged to be nonzero for all tasks, but with potentially different weights
- + intuitive for **political preference inference**

Voting intention inference performance

Root Mean Squared Error 2 2 1



UK

Mean poll Last poll Elastic Net (words) **BEN BGL**

Voting intention inference performance





Voting intention comparative plots





Voting intention comparative plots





Qualitative insights

Party	Tweet	Score	User type
SPÖ centre	Inflation rate in Austria slightly down in July from 2.2 to 2.1%. Accommodation, Water, Energy more expensive.	0.745	Journalist
ÖVP centre right	Can really recommend the book "Res Publica" by Johannes #Voggenhuber! Food for thought and so on #Europe #Democracy	-2.323	Normal user
FPÖ far right	Campaign of the Viennese SPO on "Living together" plays right into the hands of right- wing populists	-3.44	Human rights
GRÜ centre left	Protest songs against the closing-down of the bachelor course of International Development: <link/> #ID_remains #UniBurns #UniRage	1.45	Student Union

Inferring user-level information from user-generated content



Preotiuc-Pietro, Lampos & Aletras (ACL 2015) Preotiuc-Pietro, Volkova, Lampos, Bachrach & Aletras (PLOS ONE, 2015) Lampos, Aletras, Geyti, Zou & Cox (ECIR 2016)

Linguistic expression and demographics

"Socioeconomic variables are influencing language use."

(Bernstein, 1960; Labov, 1972/2006)

- + **Validate this hypothesis** on a broader, larger data set using social media
- + Applications
 - > research, as in computational social science, health, and psychology

> commercial

Standard Occupational Classification (SOC)

Major Group 1 (C1): Managers, Directors and Senior Officials Sub-major Group 11: Corporate Managers and Directors Minor Group 111: Chief Executives and Senior Officials Unit Group 1115: Chief Executives and Senior Officials •Job: chief executive, bank manager Unit Group 1116: Elected Officers and Representatives Minor Group 112: Production Managers and Directors Minor Group 113: Functional Managers and Directors Minor Group 115: Financial Institution Managers and Directors Minor Group 116: Managers and Directors in Transport and Logistics Minor Group 117: Senior Officers in Protective Services Minor Group 118: Health and Social Services Managers and Directors Minor Group 119: Managers and Directors in Retail and Wholesale Sub-major Group 12: Other Managers and Proprietors Major Group (C2): Professional Occupations •Job: mechanical engineer, pediatrist Major Group (C3): Associate Professional and Technical Occupations •Job: system administrator, dispensing optician Major Group (C4): Administrative and Secretarial Occupations •Job: legal clerk, company secretary Major Group (C5): Skilled Trades Occupations •Job: electrical fitter, tailor Major Group (C6): Caring, Leisure and Other Service Occupations •Job: nursery assistant, hairdresser Major Group (C7): Sales and Customer Service Occupations •Job: sales assistant, telephonist Major Group (C8): Process, Plant and Machine Operatives •Job: factory worker, van driver Major Group (C9): Elementary Occupations •Job: shelf stacker, bartender

provided by the Office for National Statistics (UK)

9 major groups

25 sub-major groups

90 minor groups

369 unit groups

Standard Occupational Classification (SOC)

The 9 major occupational classes (C1-9)

- **C1** Managers, Directors & Senior Officials (chief executive, bank manager)
- **C2** Professional Occupations (postdoc, pediatrist)
- **C3** Associate Professional & Technical (system administrator, dispensing optician)
- **C4** Administrative & Secretarial (legal clerk, secretary)
- **C5** Skilled Trades (electrical fitter, tailor)
- **C6** Caring, Leisure, Other Service (nursery assistant, hairdresser)
- C7 Sales & Customer Service (sales assistant, telephonist)
- **C8** Process, Plant and Machine Operatives (factory worker, van driver)
- **C9** Elementary (shelf stacker, bartender)

Forming a Twitter user data set

- + **5,191** Twitter users mapped to their occupations, then mapped to one of the 9 SOC categories
- + 10 million tweets
- + Download the data set



% of users per SOC category

Twitter user attributes (18 in total)

number of



- followers
- friends
- followers/friends (ratio)
- times listed
- tweets
- favourites (likes)
- unique @-mentions
- tweets/day (avg.)
- retweets/tweet (avg.)

Similarly to our paper for user impact estimation

proportion of

- retweets done
- non duplicate tweets
- retweeted tweets
- hashtags
- tweets with hashtags
- tweets with @-mentions
- @-replies
- tweets with links
- tweets in English

(Lampos et al., 2014)

Twitter user discussion topics (I)

Topics — Word clusters (#: 30, 50, 100, 200)

- + SVD on the graph laplacian of the word by word similarity matrix using normalised PMI, i.e. a form of spectral clustering (Bouma, 2009; von Luxburg, 2007)
- + Word2vec (skip-gram with negative sampling) to learn word embeddings; pairwise cosine similarity on the embeddings to derive a word by word similarity matrix; then spectral clustering on the similarity matrix (Mikolov et al., 2013)

Twitter user discussion topics (II)

Topic	Most central words; <i>Most frequent words</i>		
Arts	archival, stencil, canvas, minimalist; art, design, print		
Health	chemotherapy, diagnosis, disease; <i>risk, cancer, mental, stress</i>		
Beauty Care	exfoliating, cleanser, hydrating; <i>beauty, natural, dry, skin</i>		
Higher Education	undergraduate, doctoral, academic, students, curriculum; <i>students, research, board, student, college, education, library</i>		
Football	bardsley, etherington, gallas; <i>van, foster, cole, winger</i>		
Corporate	consortium, institutional, firm's; <i>patent, industry, reports</i>		
Elongated Words	yaaayy, wooooo, woooo, yayyyyy, yaaaaay, yayayaya, yayy; <i>wait, till, til, yay, ahhh, hoo, woo, woot, whoop, woohoo</i>		
Politics	religious, colonialism, christianity, judaism, persecution, fascism, marxism; <i>human, culture, justice, religion, democracy</i>		



<u>Formally</u>: Sets of random variables any finite number of which have a **multivariate Gaussian distribution**

Why do we use Gaussian Processes?

- + Kernelised, models nonlinearities
- + Interpretability (AutoRelevance Determination)
- + Performance

(Rasmussen & Williams, 2006)

More information about Gaussian Processes

- + Book: "Gaussian Processes for Machine Learning" http://www.gaussianprocess.org/gpml/
- + Video-lecture: "Gaussian Process Basics"
 http://videolectures.net/gpip06_mackay_gpb/
- + Tutorial tailored to statistical NLP tasks: "Gaussian Processes for Natural Language Processing" http://people.eng.unimelb.edu.au/tcohn/tutorial.html
- + Software I *GPML* for Octave or MATLAB http://www.gaussianprocess.org/gpml/code
- + Software II GPy for Python
 http://sheffieldml.github.io/GPy/

Gaussian Process classifier

$$k_{\text{ard}}(\boldsymbol{x}, \boldsymbol{x}') = \sigma^2 \exp\left[\sum_{i}^{d} -\frac{(x_i - x'_i)^2}{2l_i^2}
ight]$$

- Squared-exponential ARD covariance function: determines (quantify) the relevancy of each user feature, *i.e.* the relevance of feature *i* is inversely proportional to the length-scale hyper-parameter *l_i*
- + 9-class classification using one vs. all
- GP hyper-parameter learning with Expectation
 Propagation
- + Inference using **FITC** (500 inducing points)

Occupation classification performance



Occupation classification performance



Occupation classification performance



Occupation classification insights (I)



CDF of the topic "**Higher Education**": Topic **more prevalent in the upper classes** (C2, which includes education professionals, and C1), and less so in the lower classes

Occupation classification insights (II)

Arts (#116)



CDF of the topic "Arts": Topic more prevalent in C5 (which includes artists) and the upper classes

Occupation classification insights (II)

Arts (#116)



CDF of the topic "**Arts**": Topic **more prevalent in C5** (which includes artists) and **the upper classes**

Occupation classification insights (III)



CDF of the topic **"Elongated Words"**: Topic **more prevalent in the lower classes**, and less so in the upper classes

Occupation classification insights (III)



CDF of the topic "Elongated Words": Topic more prevalent in the lower classes, and less so in the upper classes

Occupation classification insights (IV)



Topic distribution distance (*Jensen-Shannon divergence*) for the different occupational classes (1-9)

Occupation classification insights (IV)



Topic distribution distance (*Jensen-Shannon divergence*) for the different occupational classes (1-9)

Occupation classification insights (IV)



Topic distribution distance (*Jensen-Shannon divergence*) for the different occupational classes (1-9)



Topic scores for occupational class supersets

Additional 'perceived' user features

- + Previously used features: **Profile** features, **Shallow** profile features, and **Topics**
- + Based on the work of *Volkova et al. (2015)*, we also incorporated:
 - > Inferred Psycho-Demographic features (15) e.g. gender, age, education level, religion, life satisfaction, excitement, anxiety etc.
 - > Emotions (9)

e.g. positive / negative sentiment, joy, anger, fear, disgust, sadness, surprise etc.

Defining the user income regression task

Group 112: Production Managers and Directors (50,952 GBP/year)

•Job titles: engineering manager, managing director, production manager, construction manager, quarry manager, operations manager

Group 241: Conservation and Environment Professionals (53,679 GBP/year)

•Job titles: conservation officer, ecologist, energy conservation officer, heritage manager, marine conservationist, energy manager, environmental consultant, environmental engineer, environmental protection officer, environmental scientist, landfill engineer

Group 312: Draughtspersons and Related Architectural Technicians (29,167 GBP/year)

•Job titles: architectural assistant, architectural, technician, construction planner, planning enforcement officer, cartographer, draughtsman, CAD operator

Group 411: Administrative Occupations: Government and Related Organisations (20,373 GBP/year)

•Job titles: administrative assistant, civil servant, government clerk, revenue officer, benefits assistant, trade union official, research association secretary

Group 541: Textiles and Garments Trades (18,986 GBP/year)

•Job titles: knitter, weaver, carpet weaver, curtain maker, upholsterer, curtain fitter, cobbler, leather worker, shoe machinist, shoe repairer, hosiery cutter, dressmaker, fabric cutter, tailor, tailoress, clothing manufacturer, embroiderer, hand sewer, sail maker, upholstery cutter

Group 622: Hairdressers and Related Services (10,793 GBP/year)

•Job titles: barber, colourist, hair stylist, hairdresser, beautician, beauty therapist, nail technician, tattooist

Group 713: Sales Supervisors (18,383 GBP/year)

•Job titles: sales supervisor, section manager, shop supervisor, retail supervisor, retail team leader

Group 813: Assemblers and Routine Operatives (22,491 GBP/year)

•Job titles: assembler, line operator, solderer, quality assurance inspector, quality auditor, quality controller, quality inspector, test engineer, weightbridge operator, type technician

Group 913: Elementary Process Plant Occupations (17,902 GBP/year)

•Job titles: factory cleaner, hygene operator, industrial cleaner, paint filler, packaging operator, material handler, packer

Same Twitter data set as in the job classification task

Use an income mapping from SOC to create real-valued target data for the regression task

User income regression: data

- + 5,191 Twitter users mapped to their occupations, then mapped to an average income in GBP (£) using the SOC taxonomy
- + ~ 11 million tweets
- + Download the data







Feature Categories

Income inference error (Mean Absolute Error) using GP regression or a linear ensemble for all features

User income regression insights (I)



User income regression insights (II)

Relating income and user attributes



Linear vs GP fit

User income regression insights (III)

Relating income and emotion



Linear vs GP fit

User income regression insights (IV)

Relating income and topics of discussion



Linear vs GP fit



 Standard Occupational Classification job groups
 National Statistics Socio-Economic Classification: Map from the job groups in the SOC to a socioeconomic status (SES): upper, middle or lower

UK Twitter user data set for SES classification

- + 1,342 UK Twitter user profiles
- + 2 million tweets
- + Date interval: Feb. 1, 2014 to March 21, 2015
- Labelled with a socioeconomic status (SES),
 using the occupational class proxy from SOC and
 NS-SEC: upper, middle, or lower
- + 1,291 **user features** following the previous paradigms, *i.e.* quantifying behaviour, impact, profile info, text in tweets and topics from tweets
- + Download the data set

SES classification performance





... using a Gaussian Process classifier

Classification	Accuracy (%)	Precision (%)	Recall (%)	F1
2 classes	82.05 (2.4)	82.2 (2.4)	81.97 (2.6)	.821 (.03)
3 classes	75.09 (3.3)	72.04 (4.4)	70.76 (5.7)	.714 (.05)

Conclusions — Mining socio-political and socio-economic signals from social media



Further thoughts

- + User-generated content is a valuable asset
- + Nonlinear models tend to perform better given the multimodality of the feature space
- + **Deeper representations** of text tend to improve performance
- + Qualitative analysis is important
 - > Evaluation
 - > Interesting insights

Some of the future research challenges

- + Work closer with **domain experts**
- + Better understanding of online media **biases**, *e.g.* demographics, external influence etc.
- + **Generalisation**, defining **limitations**, more rigorous **evaluation** frameworks
- + Methodological improvements
- + Ethical concerns

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Thank you! Any questions?

Slides can be downloaded from lampos.net/talks

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